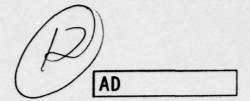


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A COMPUTER METHOD FOR THE CALIBRATION OF A PHOTOGRAPHIC EMULSION FOR SPECTROGRAPHIC ANALYSIS

BERNARD H. STRAUSS
POLYMER AND CHEMISTRY DIVISION

January 1977



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FOR THE CALIBRATION OF

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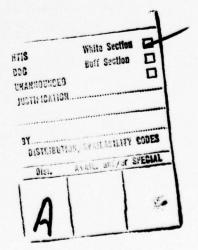
ABSTRACT

A computer method to calibrate emulsion-covered glass plates used to interpret densities of lines for quantitative spectrographic work is reported. This method follows a slightly modified ASTM graphic method, which is also described, and allows one to simply input dark and light data points to establish preliminary and emulsion calibration curves. After the curves are established, by inputting percent transmission data pairs for a known or unknown concentration line and an internal standard line, one obtains the relative intensity. The computer method is used on a Hewlett-Packard Calculator 9830-A and a UNIVAC 1108 time-sharing computer. Programs for both computers are included in this report.

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INTRODUCTION

In the past ten years, many reports have been published concerning the application of computer programming for the calibration of photographic emulsions. Calculating boards¹ and rules² have essentially been replaced by readouts from large and small computers. Authors have generally chosen to use programs that follow graphical methods of calibration, 3-8 although some, like Margoshes and Rasberry, 9 take a different approach by assuming a linear relation between functions of the relative exposure and of the microphotometer readings. Most graphic methods studied appeared to be unduly complex; for example, data was generally converted to Seidel or "modified" Seidel transformations, the use of the principles involved in Kaiser transformations were employed, or dedicated computers were used.

Our laboratory has striven for a program that would follow our present, slightly modified ASTM method of calibration which is simple in principle. We sought a computer method that would plot preliminary and emulsion calibration curves so that a convenient check could be made on the original data at any time desired. By retaining the ability to have curves printed by the computer one can decide, for instance, whether more points are needed to establish the preliminary curve, as it must be remembered that the accuracy of the final readout of any computer program is limited by the accuracy, number, and selectiveness of the original dark/light data read from the microphotometer.

Using our program, dark/light data are inputted to obtain the emulsion calibration equation. This equation is then stored either in the memory of the calculator or on recording tape. To find a relative intensity, percent transmission readings (one from the element in question and the other from an internal standard) are entered in the computer. Troubleshooting the emulsion calibration is simplified by printing the preliminary curve with the original data superimposed on it along with the emulsion calibration curve.

Two similar programs were originated to follow our existing "hand emulsion calibration" method. One program uses time-sharing computer facilities and has the capability of printing charts or tables of percent transmission and corresponding relative intensities. The other program uses a Hewlett-Packard (H.P.) 9830-A calculator with an 8K memory storage. An X-Y plotter is attached to plot curves originated by the data from the computer.

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- 10. Methods for Emission Spectrochemical Analysis. American Society for Testing and Materials, 1971.

PROCEDURE FOR EMULSION PLATE CALIBRATION

Cassette, rotation, and position settings on the spectrograph were adjusted so that the wavelength region 2750 to 3450 Å could be photographed. A solution containing 50 mg/ml iron was sparked for a twenty- and forty-second exposure. Details concerning the parameters used for excitation and conditions set on the spectrograph are found in Appendix A. A seven-step filter, with segments in the ratio of 1:2, was placed between the spark and the entrance slit of the spectrograph to stepwise attenuate the exposure.

Using a densitometer, lines on the photographic plate in the wavelength region 3000 to 3200 Å were examined. Transmittances between 1.5% and 92% in the 66% and 33% portion of a line (the second and third step of the filter) were listed in a table labeled DARK percent T and LIGHT percent T. The preliminary curve (PC) is generated from data which consists of about 50 line pairs plotted and connected on linear graph paper. Paper 15" x 10" in size was labeled DARK percent T on the ordinate and LIGHT percent T on the abscissa. Formation of this curve is the first stage in the ASTM method.

The second stage of the method is the construction of the emulsion calibration or H and D curve and it is the equation of this curve that is ultimately used in relating percent transmission to relative intensity. To construct this curve a new table was established using the two parameters, percent T and NUMBER. A DARK percent T point was chosen on the preliminary curve as low in value as possible but above the intercept of the curve with the ordinate. A corresponding LIGHT percent T point was obtained and this value was written under percent T and 7 under NUMBER as in the table. Allowing the value of the LIGHT percent T to equal the numerical value of a DARK percent T point, a new LIGHT percent T value was obtained from the PC. In the table, 6 was placed under NUMBER and the new LIGHT percent T value recorded. This method was continued until LIGHT percent T values were obtained for the corresponding numbers 5, 4, 3, and 2.

Using standard size 8-1/2- x 11-inch, two-cycle semilog paper, the ordinate or \log scale was labeled percent T (1-100) and the linear portion or abscissa was marked off from left to right, one to eight with ten divisions between marks. This axis was labeled NUMBER. Values from the table were plotted and a straight line was drawn connecting the two points corresponding to the values of 6 and 7 and extending to the abscissa axis. After establishment of this line, intermediary points between NUMBERS are taken so that the calibration curve can be drawn more accurately. This was accomplished by choosing an abscissa value between 7 and 8, for example, 7.5, and obtaining the corresponding percent T value from the straight line drawn on the emulsion calibration curve. This value was set equal to a DARK percent T point on the PC and referring back to that curve a corresponding LIGHT percent T value was determined. In the previously established table, place the value 6.5 under NUMBER (6.5 chosen because it is one less than 7.5, the starting value) and the newly obtained LIGHT percent T value under percent T. Continuing, let this new LIGHT percent T value equal that of a DARK percent T point on the PC and obtain a new LIGHT percent T number from the PC. In the table, place 5.5 under NUMBER and the newly obtained LIGHT percent T value under percent T. This procedure is continued until values have been added to the table for NUMBERS 4.5, 3.5, and 2.5. Additional starting

points such as 7.8, 7.6, etc., were chosen and the above example was followed to obtain numerous data points in order to precisely draw the emulsion calibration curve. Typical data points used to establish the preliminary and emulsion calibration curves are shown in Tables 1 and 2.

The emulsion calibration curve just completed was expanded to 15" x 10" semilog paper. The ordinate remained the same scale; however, the abscissa was expanded in such manner that two curves were plotted, one over the other. The NUMBER or abscissa axis scale is enlarged so that the NUMBERS 5 to 8 on the small calibration curve were expanded to full scale for the new curve. Starting with 5, each major division is in tenths and each minor division is equal to 0.02. The top abscissa of the new emulsion calibration curve expands the scale of the small calibration curve region NUMBERS 2 to 5 to full scale. The enlarged curve is completed using values from the table used to construct the small calibration curve.

The last stage of the calibration process involves construction of a rule. A cardboard approximately 28" x 1.5" is used as the starting material and a line is drawn dividing the cardboard in half in the long direction. Abscissa axis NUMBERS 2.0, 3.0, 4.0, 5.0, 6.0, and 7.0 are superimposed on the rule from the expanded calibration curve and marked off from the underside of the long line of the rule. This is done in such manner that approximately abscissa axis NUMBER 7.5 would be the last point at the right hand end of the rule.

With the rule aligned so that NUMBERS 7, 6, and 5 on the graph paper are in line with their corresponding NUMBERS on the rule, a right triangle is used to help superimpose the percent T ordinate values of the large emulsion calibration curve onto the rule and to mark off percent T readings on the upperside of the straight line of the rule. For example, using 2 percent T, one finds the intersection of the ordinate point 2% with the curve, aligns the long straight edge of the triangle at this point while the base of the triangle is parallel with the straight line of the rule, an alignment mark is made, and the NUMBER 2.0 is labeled. In this manner, percent transmissions between 2.0 and approximately 60.0 were marked off. The rule was then shifted so that abscissa axis NUMBERS 2.0, 3.0, and 4.0 on the calibration curve were aligned with the corresponding numbers on the rule and the remainder of the percent T scale was superimposed. The rule has the approximate range 92.0 to 2.0 percent transmission.

Table 1. TYPICAL RAW DARK AND LIGHT DATA POINTS USED TO ESTABLISH THE PRELIMINARY CURVE EQUATION

F	oint	Dark	Light
	1	8.7	24.5
	7	5.1	14.7
	14	42.1	77.1
	15	65.1	91.9
	19	11.1	29.1
	20	59.5	85.8
	30	49.7	81.1
	34	30.5	58.1
	53	38.1	73.3
	73	2.9	6.2

Table 2. TYPICAL LOG PERCENT TRANSMISSION AND NUMBER VALUES FOR ESTABLISHING THE EMULSION CALIBRATION EQUATION

Point	Log Percent Transmission	Percent Transmission 2.54	
7	0.4047		
6.6	0.5671	3.69	
6.2	0.7295	5.36	
5.8	0.8917	7.79	
5.4	1.0528	11.29	
5.2	1.1328	13.58	
4.8	1.2907	19.53	
4.3	1.4806	30.24	
3.7	1.6859	48.52	
3.3	1.7974	62.72	
2.5	1.9318	85.47	

After establishing the rule, one is then ready to interpret densitometer readings of lines on photographic plates in the calibrated wavelength region, corresponding to elements under study. A percent T for the known and for the internal standard is read from the glass emulsion. Going to the rule, and using an ordinary ruler graduated in 24 units to the inch which corresponds to the linear axis spacing on the semilogarithmic paper recommended, the relative intensity difference can be obtained. By setting the zero on the left end of the ruler on the higher percent T, one then notes the point on the ruler which corresponds to the other percent T. That number is the relative intensity for that pair of percent T values. Continuing this process for pairs of known and internal standard lines, an analytical curve can be established on semilog paper with the log axis labeled CONCENTRATION and the linear axis RELATIVE INTENSITY. From this curve unknown concentrations with known relative intensities can be determined. Typical preliminary and emulsion calibration curves and a rule are shown in Figures 1 to 3.

HEWLETT-PACKARD CALCULATOR METHOD

The equation of the preliminary curve can be determined and the curve generated by a plotter by the use of the polynomial regression procedure outlined in the MATH PAC book furnished with the H.P. computer. 11 Following this method one inputs a set of data points (Figure 4), and coefficients of a polynomial up to the 20th degree using a least-square fit may be produced. The DARK percent T and LIGHT percent T data used to draw the preliminary curve (see method done by hand) was entered into the H.P. program. Various degrees of the polynomial were

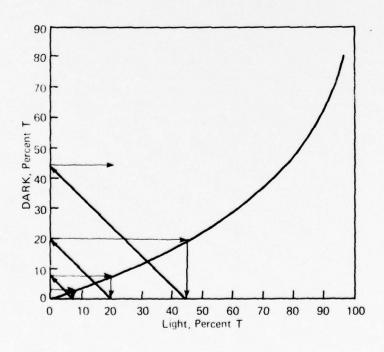


Figure 1. Preliminary curve, exemplifying method of successive determination of DARK <u>%T</u> and LIGHT <u>%T</u> values.

11. 9830 A MATH PAC, Model 30, Hewlett-Packard Calculator, v. 1.

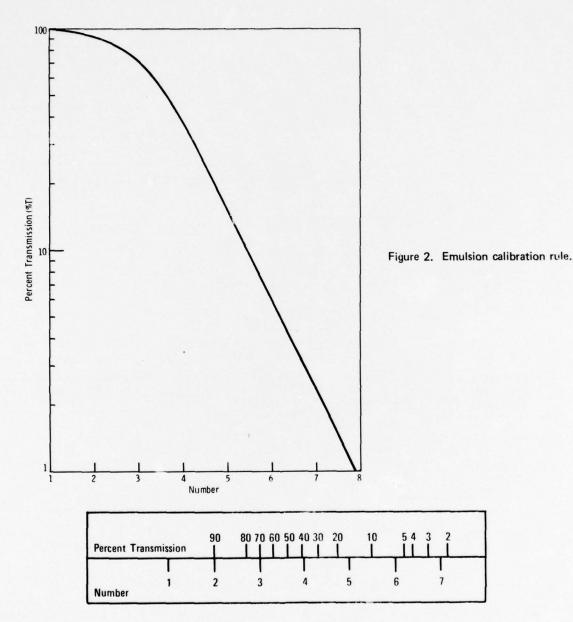


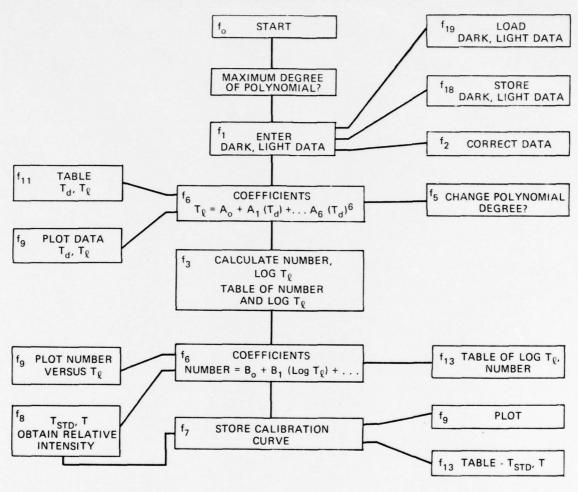
Figure 3. Condensed rule.

examined and it was found that a 6th degree gave a sufficiently high correlation coefficient for use. The following equation was used:

$$T_1 = A_0 + A_1 (T_d) + ... A_6 (T_d)^6$$

where T_1 = percent transmission of light line T_d = percent transmission of dark line A_0 , A_1coefficients of polynomial equation.

H. P. CALCULATOR OPERATIONS CHART



 T_{Q} = Percent transmission of light line

T_d = Percent transmission of dark line

Figure 4. H.P. calculator operations chart.

The data outputted contained DARK percent T values beginning with the number 1 and incremented in units of 1 to 80 along with corresponding LIGHT percent T values which are the calculated value for each DARK percent T point. Plotting the data, a smooth curve was obtained. This curve was superimposed on a hand-drawn curve from the original data and was found to be essentially identical.

Using the coefficients of the 6th degree polynomial, one generates a table labeled LIGHT percent T and NUMBER which is used to formulate the emulsion calibration curve. Referring to the above equation, let T_d equal 1, solve the above equation for T_1 and store this value in the table along with the NUMBER 7. The computer sets $T_d = T_1$ and resolves the equation. In this manner, values in the table for T_1 are established for NUMBERS 7, 6, 5, 4, 3, and 2.

A linear curve is assumed between the data points NUMBER = 7, percent T = value found, and NUMBER = 6, percent T = value found. The straight line region is extended to percent T = 1, NUMBER = calculated value from the equation of the straight line. Solving this straight line equation, the computer is then able to take NUMBER values along this line and obtain corresponding T_1 values. For example, using the NUMBER value 7.5, a corresponding T_1 value is obtained from the equation of the straight line. This is set equal to T_d and placed in the previous polynomial equation:

$$T_1 = A_0 + A_1 (T_d) + ... A_6 (T_d)^6$$

and a corresponding T_1 value is received. In the table T_1 and NUMBER, the T_1 value obtained and the NUMBER 6.5 (one less than 7.5), are stored. In similar fashion, NUMBER values from 6.9 to 2.1 in increments of one tenth are obtained.

The data from the table LIGHT percent T versus NUMBER is then used to generate the coefficients for the equation:

NUMBER =
$$B_0 + B_1 (\log T_1) + ... B_6 ((\log T_1)^6)$$
.

A 6th degree polynomial furnished a high correlation coefficient.

Using the above equation, percent T for a known element (obtained from the density of the line on the glass plate emulsion) is substituted for the T_1 value. Solving the equation a value for NUMBER is obtained. The procedure is repeated for a percent T for an internal standard and another NUMBER is obtained. The computer subtracts these two NUMBERS and their difference is called RELATIVE INTENSITY. As outlined in the method done by hand, this process is continued for pairs of known and internal standard lines. An analytical curve is established on semilog paper with the log axis labeled CONCENTRATION and the linear axis RELATIVE INTENSITY. From this curve unknown concentrations with known relative intensities can be determined. Program used is presented in Appendix B.

UNIVAC 1108 COMPUTER METHOD

Appendix C lists the UNIVAC 1108 program. The only input necessary for the program is the initial DARK/LIGHT data read from the emulsion-covered glass plate used for the calibration. Using these values, the computer can calculate coefficients of a polynomial equation to any practical degree required, and from the values obtained, the lowest degree polynomial with good correlation coefficient was chosen. The program then outputted least-square data of DARK/LIGHT points, that is DARK, LIGHT, and LIGHT FITTED, from which the preliminary curve may be drawn. If desired, a plot of this curve can be obtained.

Following the procedure outlined in the Hewlett-Packard Calculator Method, a table labeled LIGHT percent T and NUMBER is generated to formulate the coefficients of the emulsion calibration equation used as the equation of the emulsion calibration curve.

NUMBER = $B_0 + B_1 (\log T_1) + B_n (\log T_1)^n$

where T_1 = percent transmission of light line $B_0...B_n$ = coefficients of polynomial equation.

After determining the coefficients of the above equation with the UNIVAC 1108, the equation can be used with many small desk top calculators that do not have the memory needed to solve a 6th degree polynomial. By inserting the log of the percent transmission of an elemental line, one gets the value for NUMBER.

Assuming a calculator is not available, using the above equation, a chart of percent transmission and NUMBER may be generated. Percent T was varied in increments of 0.05 from 2 to 20 and in units of 0.1 from 20 to 90. The left vertical column of the chart lists changes in percent transmission by one unit, for example, from 20 to 21. The top row of the chart varies percent T by either 0.05 or 0.1 depending on the percent transmission range. The body of the chart contains NUMBER values. For example, if an intensity of an element of a standard sample line was measured at 50.5% T and that of an element internal standard line at 20.6% T, one would find the corresponding NUMBER value by proceeding horizontally along the chart from the extreme left column containing the number 50 as the first integer until one reaches the column headed by 0.5. This NUMBER value is then recorded. The procedure is repeated for the other transmission value of 20.6. The difference in NUMBER values is the relative intensity.

Various harts were attempted, including one in which two percent transmissions (for example, from the unknown element line and that of the internal standard) could be found in the first column and first row of the chart. The point of intersection, going horizontally and vertically along the chart from the two percent T values, is the relative intensity and the need of taking the difference in NUMBER for each percent T pair is eliminated. To accomplish this, however, the chart became very voluminous and it was found that the previously described chart was easier to use.

CONCLUSION

A computer program that follows closely the ASTM graphic method has been developed for use on a Hewlett-Packard 9830-A and a UNIVAC 1108 time-sharing computer. For laboratories that do not have continuous access to these computers, one can obtain the coefficients to the equation relating percent transmission to relative intensity and then use the equation on small memory desk top calculators to find relative intensities.

The program used in the UNIVAC 1108 will output a table of percent transmission versus NUMBER which is used to obtain the relative intensity for a pair of percent transmission values.

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A COMPUTER METHOD FOR THE CALLBRATION OF A PHOTOGRAPHIC EMULSION FOR SPECTROGRAPHIC ANALYSIS - Bernard H. Strauss WATERTOWN, MASSACHUSETTS 02172 A COMPUTER METHOD FOR THE CALIBRATION OF A PHOTOGRAPHIC EMULSION FOR SPECTROGRAPHIC Army Materials and Mechanics Research Center, ANALYSIS - Bernard H. Strauss computer Amy densities of lines for quantitative spectrographic work is reported. This method follows a slightly modified ASTM graphic method, which is also described, and allows one to simply input dark and light data points to establish preliminary and emulsion calibration curves. After the curvers are established, by inputting percent transmission data pairs for a known or unknown concentration line and an internal standard line, one obtains the relative intensity. The computer method is used on a Hewlett-Packard Calculator 9830-A and a UNIVAC 1108 time-sharing computer. Programs for both computers are included in this report. A computer method to calibrate emulsion-covered glass plates used to interpret densities of lines for quantitative spectrographic work is reported. This method follows a slightly modified ASIM graphic method, which is also described, and allows one to simply input dark and light data points to establish preliminary and emulsion calibration curves. After the curves are established, by inputiting percent transmission data pairs for a known or unknown concentration line and an internal standard line, one obtains the relative intensity. The computer method is used on a Hewlett-Packard Calculator 9830-A and a UNIVKC 1108 time-sharing computer. Programs for both computers are included in this report. Spectrographic analysis Calibrating Spectrographic analysis UNLIMITED DISTRIBUTION UNCLASSIFIED
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APPENDIX A. SPECTROGRAPHIC PARAMETERS

Equipment

Baird 3-meter spectrograph, 2.75 Å/mm reciprocal linear dispersion Jarrell-Ash Varisource Jarrell-Ash Microphotometer

Instrumental Parameters

Spark-18,000 V. A. C., 3 breaks per half-cycle, 6 to 6.5 amperes Analytical gap-3 mm Auxiliary gap-6 mm Sample electrode-Ultra Carbon 106 Counter electrode-Ultra Carbon 105 U Pre-spark duration-20 sec.

Photographic Parameters

Plates-Eastman Kodak SA l Developer-Eastman Kodak D19 Developing time- 3.5 min. Developing temperature 20°C

Spectral range of calibration 2750-3450 Å Spectral lines read in range of 3000-3200 Å

APPENDIX B. HEWLETT-PACKARD CALCULATOR PROGRAM FOR GLASS PLATE EMULSION CALIBRATION

```
For 1=1 to 22
    10
                                                          30
                                                                 End
    20
          C[I] = B[I] = 0
                                                                 Disp " Wrong No., Dark, Light =";
                                                          40
          Next 1
    30
                                                          50
                                                                 Input 1, Y, B [2]
          For 1 = 23 to 253
    40
                                                                 G[I] = Y
                                                          60
          C[1] = 0
    50
                                                          70
                                                                 H[1] = B[2]
          Next 1
    60
                                                          80
                                                                 Print "Delete: Dark = "G[I]" Light = "H [I]
          B[1] = 1
    70
                                                          90
                                                                 Y = FNX (-1)
          W = N = S1 = S2 = S3 = S4 = S5 = 11 = 0
                                                          100
                                                                 Disp
          Disp " Max Degree Polynomial ";
    90
                                                          110
                                                                 End
                                                       f_3
    100
          Input D2
          Print " Max Degree Polynomial = " D2
    110
                                                          10
                                                                 11 = 0
    120
                                                          20
                                                                 Print " Polynomial Degree = "DI
    130
          Print
                                                          30
                                                                 Print "Relative | Log T Light "
    140
          End
                                                          40
                                                                 X2 = 1
f
                                                                 X = 1
                                                          50
    10
          Format F 4.0, 2 F 12.4
                                                          60
                                                                 x1 = 8
    20
          Print "Enter Prelim Calibro Data"
                                                          70
                                                                 If X1 < = 2 then 210
          If N ≠ 0 then 70
                                                          80
                                                                 Y = B[DI +1]
    40
          Print "No." Tab 10" Dark "Tab 22 "Light"
                                                                 For J = DI to 1 Step -1
                                                          90
    50
          11 = 0
                                                          100
                                                                 Y = Y * X + B[J]
    60
          11 = 11 + 1
                                                          110
                                                                 Next J
                                                                 X=Y
    70
          Disp "Dark, Light =";
                                                          120
                                                                 If X>100 then 210
    80
          Input G[11], H [11]
                                                          130
           Y = H[11]
                                                          140
                                                                 X1 = X1-1
    90
           B[2] = G[11]
                                                                 If X1 < = 2 then 210
    100
                                                          150
          Write (15, 10) N+1, G [11], H [11]
                                                          160
                                                                 11 = 11 + 1
    110
          Y = FN \times 1
                                                          170
                                                                 H[11] = X1
    120
                                                                 G [11] = L G T X
                                                          180
    130
          Go to 60
    140
          End
                                                          190
                                                                 Print X1, G [11], X
f2
                                                          200
                                                                 Go' to 70
                                                                 x2 = x2 - 0.1
    10
           If W = 0 then 40
                                                          210
          Disp " Not allowed"
                                                          220
                                                                 If X2 = 0 then 290
    20
                                                          230
                                                                 11 = 11 + 1
```

```
G[11] = (G[2] - G[3]) * X2 + G[2]
                                                              Disp " Max Deg ="; D2 - W
240
                                                       30
                                                       40
250
       X1 = 6 + X2
                                                               If W = 0 then 330
                                                       50
       X = 10+G [11]
260
                                                       60
                                                              T = 0
270
       H[11] = X1
                                                              For 1 = 1 to 01 + 1
                                                       70
       Go to 190
280
                                                       80
                                                              B[I] = 0
       Y = FN Y1
290
                                                              For J = 1 to D1 - 1 + 2
                                                       90
300
       End
                                                       100
                                                              R = (I + J - 1) * D2 + 2 - 0.5 * (I + J))
                                                              B[I] = B[I] + C[T + J] + C[R]
                                                       110
       Def FNX (Z)
10
                                                       120
                                                              Next J
       For I = 2 to D2
20
                                                              T = 1 \div (D2 + (3-1) / 2)
                                                       130
       B[I+1] = B[I] * B[2]
30
                                                       140
                                                              Next I
40
       Next I
                                                              R1 = 0
                                                       150
       B [D2 + 2] = Y
50
                                                       160
                                                              For 1 = 2 to 01 + 1
       R = 0
60
                                                       170
                                                              R1 = R1 + C [1*(D2 + (3-1) / 2]+2
      For 1 = 1 to 02 + 2
70
                                                       180
80
      For J = 1 to D2 + 2
                                                       190
                                                              TO = C [(02 + 1) * (02+2) / 2]
       R = R+1
90
                                                              TO = TO - C [D2 + 1]+2
                                                       200
       C[R] = C[R] + B[I] * B[J] * Z
100
                                                       210
                                                              Print
110
       Next J
                                                              Print " Coefficients"
                                                       220
       Next 1
120
                                                       230
                                                              Print
130
       SI = SI + B [2] * Z
                                                              Format F3.0, E 12.4
                                                       240
140
       S2 = S2 + B [2] + 2 * Z
                                                              For 1 = 1 to 01 + 1
                                                       250
       S3 = S3 + Y * Z
150
                                                              Write (15, 240) " B ("I-1") = "B[I]
       S4 = S4 + Y *Y * Z
                                                       260
160
       S5 = S5 + B [2] * Y * Z
                                                              Next I
170
                                                       270
180
       N = N + Z
                                                       280
                                                              Print
                                                               Print
                                                       290
190
       Return 0
                                                              Print "R Square = " R1/T0
                                                       300
10
       Disp " New Polynomial Degree =";
                                                       310
                                                              Print
       Input D1
20
                                                       320
                                                               End
       Print " Degree of Polynomial =" D1
30
                                                       330
                                                               If N > D2 then 360
40
       End
                                                       340
                                                              Disp " Not Enough Points"
                                                       350
                                                              End
10
       If N < = D2 - W then 340
                                                       360
       If D1 = D2 - W then 50
20
```

```
710
       D2 = D2 + 1
370
                                                                  Next J
380
       For J = 1 to D2
                                                           720
                                                                  Next 1
390
       Print C [P]
                                                           730
                                                                  C[1] = 1/C[1]
       C[P] = SQRC[P]
                                                           740
                                                                  Go to 60
400
       For I = 1 to D2 - J+1
410
                                                        f 7
420
       C[P+1] = C[P+1] / C[P]
                                                            10
                                                                  B [22] = D1
430
       Next I
                                                                   Print " Store X = F ( Log T) Calibration "
                                                            20
440
       R = P + I
                                                                   Disp " Store File # = ";
                                                            30
450
       S = R
                                                            40
                                                                   Input I
       For L = 1 TO D2 - J
460
                                                                   Print " Store File # " I
                                                            50
       P = P + 1
470
                                                            60
                                                                   Store Data I, B
       For M = 1 to D2 + 2 - J - L
480
                                                            70
                                                                   End
       C [ R+M - 1] + C [ R+M-1] - C [P] * C [P+M-1] f8
490
500
       Next M
                                                                   Print " Diff X Evaluation"
                                                            10
       R = R + M - 1
510
                                                            20
                                                                   Disp " T (STD), T = ";
520
       Next L
                                                                   Input T1, T2
                                                            30
530
       P = S
                                                            40
                                                                   Print " T (STD) = "T1
540
       Next J
                                                                   Print " T = " T2
                                                            50
       T = (D2 + 1) * (D2 + 2) /2
550
                                                                   T1 = LGTT1
                                                            60
560
       For 1 = 1 to D2 - 1
                                                                   T2 = LGTT2
                                                            70
570
       T = T - 1 - 1
                                                                   X1 = X2 = B [D1 + i]
580
       C[T] = 1 / C[T]
                                                                   For J = D1 to 1 Step - 1
                                                            90
590
       For J = 1 to D2 - 1
                                                                   X1 = X1 * T1 + B [J]
                                                            100
600
       P = D2 + 1 - I - J
                                                            110
                                                                   X2 = X2 * T2 + B [J]
       P = P * (D2 + 1 - (P-1)/2) - 1
610
                                                            120
                                                                   Next J
620
       R = P-J
                                                                   Print " X (STD) = " x1
                                                            130
630
       S = 0
                                                            140
                                                                   Print " X = " X2
       U = 1 + J + 1
640
                                                            150
                                                                   Print " X (STD) - X = "X1-X2
       Y = P
650
                                                            160
                                                                   Go to 20
660
       For K = 1 to J
                                                                   End
                                                            170
       Y = Y + U - K
670
                                                        f<sub>9</sub> 10
                                                                      Disp "Re-plot Axis";
       S = S - C[R+K] + C[Y]
680
                                                             20
                                                                      Input Z9
       Next K
690
                                                             30
                                                                      If Z9 = 0 then 390
```

C[P] = S / C[R]

700

```
For X = A2 to B2 Step C2/10
40
         Disp "X (Max) = ";
                                                             390
                                                                      Y = B [D1 + 1]
50
         Input B2
                                                             400
         Disp "X (Min) = ";
                                                             410
                                                                      For J = D1 to 1 Step -1
60
                                                             420
                                                                      Y = Y * X + B [J]
         Input A2
70
                                                             430
                                                                      Next J
         Disp "Y (Max) = ";
80
                                                             440
                                                                      Plot X,Y
90
         Input B1
         Disp "Y (Min) = ";
                                                             450
                                                                      Next X
100
                                                             460
                                                                      Disp "Plot Data Points";
110
         Input Al
         C2 = (B2 - A2) / 10
                                                             470
                                                                      Input Z9
120
                                                             480
                                                                      If Z9 = 0 then 550
         C1 = (B1 - A1) / 10
130
                                                             490
                                                                      PEN
         Scale A2, B2 + 2*C2, A1, B1, + 2*C1
140
                                                                      For K = 1 to 11
         Plot A2 + (B2 - A2) /2.2, A1 + C1 /4
                                                             500
150
                                                             510
                                                                      Plot G[K], H [K]
         Label (*, 3, 2, 0, 2/3)
160
                                                                      CPLOT -0.3, -0.3
                                                             520
170
         Letter
180
         Plot A2 + C2/4, A1 + (B1 -A1)/2.2
                                                             530
                                                                      Label (*) "0"
         Label (*, 3, 2, PI/ 2, 2/3
                                                             540
                                                                      Next K
190
200
         Letter
                                                             550
                                                                      PEN
220
         Offset C2, C1
                                                                      Plot -1.2 * C2, -C1
                                                             560
         XAXIS A1, C2, A2, B2
                                                                      PEN
230
                                                             570
         YAXIS B2, C1, A1, B1
                                                             580
                                                                      Go to 10
240
250
         YAXIS A2, C1, A1, B1
                                                          f 11
                                                                      Format 2F 12.4
260
         XAXIS B1, C2, A2, B2
                                                             10
                                                                      Print Tab 9 "X Dark "Tab 21" Y Light"
                                                             20
         Label (*, 2, 1.7, 0, 2/3)
270
                                                             30
                                                                      For I = 1 to 79 Step 2
         For Y = Al to Bl Step 2*Cl
280
                                                             40
                                                                      Y = B [D1 + 1]
         Plot A2, Y, 1
290
                                                             50
                                                                       For J = D1 to 1 Step -1
         CPLOT -5.4, -0.34
300
                                                             60
                                                                      Y = Y * I + B [J]
         Label (380, 2, 1.7, 0, 2/3) Y
310
                                                                      Next J
                                                             70
         Next Y
320
                                                                      Write (15, 10) 1, Y
                                                             80
         For X = A2 to B2 step 2*C2
330
                                                             90
                                                                      Next I
340
         Plot X, Al, 1
                                                             100
                                                                      For I = 80 to 100 Step 1
         CPLOT -3.8, -1
350
                                                                      Y = B [Di + 1]
                                                             110
         Label (380, 2, 1.7, 0, 2/3) X
360
                                                             120
                                                                      For J = D1 to 1 Step -1
370
         Next X
                                                                       Y = Y * I + B[J]
                                                             130
         Format F 5.1
380
```

```
Y = FN X1
                                                             190
    140
             Next J
                                                                      Print 13, G[13], H [13]
    150
             Write (15, 10) 1, Y
                                                             200
                                                             210
                                                                       1F 13 = 11 - 1  then 230
    160
             Next 1
                                                                      Go to 160
                                                             220
    170
             End
                                                             230
                                                                       End
  f<sub>13</sub>
                                                        f 17
    10
             Format 2 F 12.4
                                                             10
                                                                       Print "Load X = F (LOG T) Calibration"
    20
             Print Tab 9 "X" Tab 21 "T"
                                                                       Disp "Load File # = ";
                                                             20
             For 1 = 0.3 to 2 Step 0.05
    30
                                                             30
                                                                       Input I
             Y = B [D1 + 1]
    40
                                                                       Print "Load File # "I
                                                             40
             For J = D1 to 1 Step -1
    50
                                                             50
                                                                       Load Data I, B
             Y = Y * I + B [J]
    60
                                                                       Di = D2 = B[22]
                                                             60
             Next J
    70
                                                                       Print "Degree Polynomial = "D1
                                                             70
    80
             Write (15, 10) Y, 10+1
                                                                       End
                                                             03
             Next I
    90
                                                         f 18
    100
             End
                                                             10
                                                                       Disp "Store Data, File # = ";
f14
                                                                       Input 1
                                                             20
             Def FNY(Z)
    10
                                                             30
                                                                       Store Data I
             Disp "Max Degree Polynomial";
    20
             Input D2
    30
                                                         f<sub>19</sub>
             Print "Degree Polynomial = "D2
    40
                                                                       Disp "Load Data, File # = ";
                                                              10
             Di = D2
    50
                                                                       Input I
                                                             20
             Print II
    60
                                                                       Load Data I
                                                             30
             For 1 = 1 to 22
    70
                                                                       Format F 4.0, 2 F 12.4
                                                             40
             C[I] = B[I] = 0
    80
                                                                       Print "No." Tab 10 "Dark" Tab 22 "Light"
                                                             50
             liext 1
    90
                                                                       11 = 0
                                                             60
             For 1 = 23 to 253
    100
                                                                       11 = 11 +1
                                                             70
             c [1] = 0
    110
                                                                       Y = H [11]
                                                             80
    120
             Next 1
                                                                       B[2] = G[11]
                                                             90
    130
             13 = 0
                                                             100
                                                                       Write (15, 40) N + 1, G [11], H[11]
             B[1] = 1
    140
                                                              110
                                                                      Y = FNX1
             W = N = S1 = S2 = S3 = S4 = S5 = 0
    150
                                                             120
                                                                       Go to 70
             13 = 13 + 1
    160
                                                             130
                                                                       END
             B[2] = G[13]
    170
             Y = H [13]
    180
```

APPENDIX C. UNIVAC 1108 PROGRAM

```
DIMENSION X(1200), Y(1200), W(200), T1(200), T2(200), T3(200),
 1
       C(11), ALPHA(10), BETA(10),
       DIMENSION S(4), YF(400), A(14)
       FORMAT (/// 29H OUTPUT FROM SUBROUTINE FITY.//7H IND 3 = I 3///3X
105
       2H 1X, 18X 2HY, 14X 9H Y FITTED // (1H 1P3E 20.7))
       FORMAT (///31H OUTPUT FROM SUBROUTINE ORTHLS.//7H IND 1 = 13//2X
103
       2HI, 13X 2H C, 16X 6H ALPHA, 14X 5H BETA/1H I4, 1PE 20.7/
 1
       (1H I4, 1P3E 20.7))
104
       FORMAT (/// 30H OUTPUT FROM SUBROUTINE COEFS.//7H IND 2 = \frac{13}{13X}
       2HI, 17X 5H A(I)//(1H I14, 1PE 26.7))
       P = 3.141592654
       READ 1,N,K
       READ 1, NUM, NUMA, DUM
       FORMAT (I5, I5, F10.0)
       DO 10 I = 1, N
       READ 2, X(I), Y(I)
 10
       CONTINUE
       FORMAT (F10.0, F10.0)
101
       L = 0
       CALL ORTHLS (X, Y, W, N, L, J, C, ALPHA, BETA, K, T1, T2, T3, IND1)
       IT = 0
       WRITE (6, 103) IND 1, II, C(1), (II, C(II + 1), ALPHA (II), BETA (II),
      II = 1, K)
       DO 15 MM = 1, K
       KF = MM
       CALL FITY (X, N, J, C. ALPHA, BETA, KF, YF, T1, T2, IND 3)
       WRITE (6, 105) IND 3, (X(I), Y(I), YF(I), I = 1, N)
       CALL COEFS (J, C, ALPHA, BETA, KF, A, T1, T3, IND 2)
       WRITE (6, 104) IND2, II, A(1), II, A(II + 1),
       II = 1, KF)
 82
       FORMAT (1H1)
       FORMAT (1H 3E 15.6)
       MB = MM + 1
       CONTINUE
 15
       PRINT 82
       DO 80 IA = 1, N
       ANS = A(1)
       DO 75 II = 2, MB
       FIB = II -1
       ANS \approx ANS + A(II) *X(IA)* FIB
       IF (IT. EQ.3) X(IA) = EXP(X(IA))
       PRINT 81, X(IA), Y(IA), ANS
 80
```

```
IF, (IT.EQ.3) GO TO 102
      PRINT 82
      AB = 1.0
      SAVE = SOLVE (A, AB, MB)
      PRINT 85, SAVE, AB
      SAVE = SOLVE (A, SAVE, MB)
      PRINT 85, SAVE 1, SAVE
      CON = ALOG (SAVE)
      CON 1 = ALOG (SAVE 1)
      D = CON1 - CON
      Y(1) = ALOG (SAVE)
      X(1) = 7
      S(1) = SAVE
      DD = D/10
       DO 650 I = 2, 10
      S(I) = EXP (CON + DD * (I - 1))
      X(I) = 7. -(I-1)*.1
650
      Y(I) = ALOG(S(I))
       L = 10
       DO 651 J = 1, 10
       AB = S(J)
       DO 652 JJ = 1,4
       L = L + 1
       ANS = SOLVE (A, AB, MB)
      Y(L) = ALOG (ANS)
       X(L) = X(J) -1.0 * JJ
       IF (ANS. GE. 100.) GO TO 653
       PRINT 85, ANS, AB, X(L)
       AB = ANS
652
       GO TO 651
653
       L = L-1
651
       CONTINUE
       IT = 3
       N = L
       DO 107 J = 1, N
       TEM = X(J)
       X(J) = Y(J)
107
       Y(J) = TEM
       GO TO 101
       CONTINUE
102
       NUMB = NUM + 10
       NUMC = NUMA + 1
       DO 111 1 = 1, NUMB
       X(I) = DUM
       IF (I. GT. NUMC) X(I) = X(1) + .05
```

```
AB = ALOG(X(I))
      Y(I) = SOLVE(A, AB, MB)
111
      DUM = X(1) + .05
      PRINT 17
      WRITE (6, 18)
      DO 40 I = 1, NUMA, 20
      JJ = I + 19
 40
      WRITE (6, 19) X(1), (Y(J), J = 1, JJ)
      NUMB = JJ + 1
       IPRINT = NUMB + 500
       PRINT 17
       WRITE (6, 13)
       DO 150 I = NUMB, NUM, 10
      JJ = I + 9
       IF(I, GT. IPRINT) GO TO 16
      GO TO 150
      IPRINT = I + 500
 16
      PRINT 17
      PRINT 13
      WRITE (6,11) X(I), (Y(J), J = I, JJ)
150
      FORMAT (1H 21F6.2)
 19
 18
       FORMAT (16 X, '.05' 3X, '.10' 3X, '.15' 3X, '.20 3X, '.25'
       3X, '.30',
       3X, '.35' 3X, '.40' 3X, '.45' 3X, '.50' 3X, '.55' 3X, '.60' 3X, '.65'
       3X, '.70' 3X, '.75' 3X, '.80' 3X, '.85' 3X, '.90' 3X, '.95'
 11
       FORMAT (1H F6.2, 10F8.2)
       FORMAT (1H 19X '.1', 6X '.2', 6X '.3', 6X '.4', 6X '.5', 6X '.6',
 13
       6X '.7', 6X '.8', 6X '.9')
 17
       FORMAT (1H1)
       FORMAT (1H 'Y 1 = ' F13.8, 5X, 'X1 = ' F13.8, E14.8)
 85
       STOP
       END
       LEGEND
        N = No. OF EXPERIMENTAL POINTS
        K = MAXIMUM ORDER OF EQUATION FOR POLYNOMIAL LEAST SQUARES FIT.
        NUM = TOTAL NUMBER OF PERCENT TRANSMISSION vs RELATIVE INTENSITY VALUES
         IN TABLE
        NUMA = TOTAL NUMBER OF PERCENT TRANSMISSION VALUES OF INCREMENT .05 IN TABLE
        DUM = INITIAL VALUE OF PERCENT TRANSMISSION PRINTED IN TABLE (2.0 USED IN
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        X(I) = EXPERIMENTAL DARK PERCENT TRANSMISSION
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Y(I) = EXPERIMENTAL LIGHT PERCENT TRANSMISSION

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